# **Ch2: Robot Dynamics – Part 3**

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# **Dynamics in Task Space**



#### **Dynamics in Task Space (Based on Geometric Jacobian)**

(cont.)

By considering 
$$
c(\theta, \dot{\theta}) = C(\theta, \dot{\theta})\dot{\theta}
$$
:  
\n
$$
c_C(\theta, \mathcal{V}) = J^{-T}c(\theta, J^{-1}\mathcal{V}) - M_C(\theta)JJ^{-1}\mathcal{V}
$$
\n
$$
= J^{-T}C(\theta, J^{-1}\mathcal{V})J^{-1}\mathcal{V} - M_C(\theta)JJ^{-1}\mathcal{V}
$$
\n
$$
= (J^{-T}C(\theta, J^{-1}\mathcal{V}) - M_C(\theta)J)J^{-1}\mathcal{V}
$$
\n
$$
= C_C(\theta, \mathcal{V})\mathcal{V}
$$

**Note**: In general, we cannot replace the dependence on  $\theta$  by a dependence on the endeffector configuration  $T$  because there may be multiple solutions to the inverse kinematics, and the dynamics depends on the specific joint configuration  $\theta$ .

**Note**: For finding  $\dot{J}(\theta)$ , let  $J_i(\theta)$  denote the *i*th column of  $J(\theta) = [J_1(\theta), ..., J_n(\theta)]$ , thus:

$$
\dot{J}(\theta) = \frac{d}{dt}J(\theta) = \left[\frac{d}{dt}J_1(\theta), \dots, \frac{d}{dt}J_n(\theta)\right] \text{ where } \frac{d}{dt}J_i(\theta) = \sum_{j=1}^n \frac{\partial J_i}{\partial \theta_j} \dot{\theta}_j
$$
  
- If  $J(\theta) = J_0(\theta)$ :  

$$
\frac{\partial J_i}{\partial \theta_j} = \begin{cases} \begin{bmatrix} ad_{J_j} \end{bmatrix} J_i & i > j \\ 0 & i \le j \end{cases} \qquad \qquad \frac{\partial J_i}{\partial \theta_j} = \begin{cases} \begin{bmatrix} ad_{J_i} \end{bmatrix} J_j & i < j \\ 0 & i \ge j \end{cases}
$$

#### **Dynamics in Task Space (Based on Analytic Jacobian)**

In a similar way, by using  $\bm{J}_a(\bm{\theta})$  where  $\dot{x} = \bm{J}_a(\bm{\theta})\dot{\bm{\theta}}$  and  $\bm{\tau} = \bm{J}_a^T(\bm{\theta})\bm{F}$ , dynamic equation in T-space can be written as

> $\mathbf{F} = \mathbf{M}_C(\boldsymbol{\theta})\ddot{\mathbf{x}} + \mathbf{c}_C(\boldsymbol{\theta},\dot{\mathbf{x}}) + \mathbf{g}_C(\boldsymbol{\theta}) + \mathbf{F}_{\text{tin}}$  $= M_C(\theta)\ddot{x} + C_C(\theta, \dot{x})\dot{x} + g_C(\theta) + F_{\text{tip}}$

**Note**: All the properties of the J-space dynamic model carry over to the T-space dynamic model as long as  $J$  (or  $J_a$ ) is nonsingular. For instance,

- $M<sub>C</sub>$  is symmetric and positive definite.
- For a revolute arm,  $J$  (or  $J_a$ ) is bounded, and  $M_c$  is bounded above and below.
- ${\cal S}_c = \dot{\bm{M}}_C 2 \bm{C}_C$  is skew-symmetric (if  $\bm{C}\big(\bm{\theta},\dot{\bm{\theta}}\big)$  is in standard form).
- Property of linearity in the parameters:  $F = M_C(\theta)\ddot{x} + c_C(\theta, \dot{x}) + g_C(\theta) = J^{-T}Y(\theta, \dot{\theta}, \ddot{\theta})\pi$

 $Y_c$ 

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## **Constrained Dynamics**

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### **Constrained Dynamics**

Sometimes robots are subject to a set of constraints on their motion.

Consider the case where the  $n$ -joint robot is subject to a set of  $k$  **holonomic constraints** or **nonholonomic Pfaffian velocity constraints** of the form:

$$
A(\boldsymbol{\theta})\dot{\boldsymbol{\theta}}=\mathbf{0},\qquad A(\boldsymbol{\theta})\in\mathbb{R}^{k\times n}
$$

**Assumption**: These *k* equality constraints are workless, meaning that the forces that enforce these constraints do no work on the robot (e.g., frictionless contacts).

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### **Constrained Dynamics**

The space of joint torques/forces  $\tau$  is divided into two independent subspaces; (I) an  $(n - k)$ dimensional subspace that affects the motion of the robot, but not the constraint force (this subspace is tangent to constraint) and (II) a  $k$ -dimensional subspace that affects the constraint force, but not the motion (this subspace is against the constraints).





### **Constrained Dynamics**

Thus, the robot has  $n - k$  velocity freedoms and k force freedoms.

For finding 
$$
\lambda
$$
:   
(1)  $\rightarrow \ddot{\theta} = M^{-1}(\tau - h - A^{T}\lambda)$  (3)  
(2), (3)  $\rightarrow \lambda = (AM^{-1}A^{T})^{-1}(AM^{-1}(\tau - h) + \dot{A}\dot{\theta})$  (4)

By eliminating  $\lambda$  in (1) using (4),  $n + k$  constrained equations of motion can be reduce to the dynamics projected to the  $(n - k)$ -dimensional space tangent to the constraints, i.e., (5):

$$
\begin{cases}\n\tau = M(\theta)\ddot{\theta} + h(\theta, \dot{\theta}) + A^{T}(\theta)\lambda & \Rightarrow \mathbf{P}\tau = P(M\ddot{\theta} + h) \quad (5) \\
A(\theta)\dot{\theta} = 0 & \stackrel{(or)}{\rightarrow} \dot{A}(\theta)\dot{\theta} + A(\theta)\ddot{\theta} = 0 & \mathbf{P} = I_{n} - A^{T}(AM^{-1}A^{T})^{-1}AM^{-1} \in \mathbb{R}^{n \times n} \\
I_{n}: n \times n \text{ identity matrix}, \quad \text{rank}(P) = n - k\n\end{cases}
$$

**Note**: If the constraint acts at the end-effector of an open-chain robot, then

$$
\boldsymbol{J}^{\mathrm{T}}(\boldsymbol{\theta})\boldsymbol{\mathcal{F}}_{\mathrm{tip}} = \boldsymbol{A}^{\mathrm{T}}(\boldsymbol{\theta})\boldsymbol{\lambda}
$$
  
( $\boldsymbol{\theta}$ ) is invertible:  $\boldsymbol{\mathcal{F}}_{\mathrm{tip}} = \boldsymbol{J}^{-\mathrm{T}}(\boldsymbol{\theta})\boldsymbol{A}^{\mathrm{T}}(\boldsymbol{\theta})\boldsymbol{\lambda}$ 

 $\mathcal{F}_{\text{tip}}$ : Wrench the end-effector applies against the constraint (and it does not have component tangent to constraint).

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If  $\boldsymbol{I}$ 

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#### **Constrained Dynamics**

Therefore,

 $\tau = M(\theta)\ddot{\theta} + h(\theta, \dot{\theta}) + A^{T}(\theta)\lambda$   $\equiv$   $\tau = P(\theta)\tau + (I_n - P(\theta))\tau$ For acting against the For moving the robot constraints  $(\tau_{\rm con})$ tangent to constraint example joint torques  $\tau$ Matrix  $P(\theta)$  is a **projection matrix** that projects  $\tau$  to its  $I-P$ component tangent to the constraint, the matrix  $I_n - P(\theta)$  $(I-P)\tau$ projects  $\tau$  to its component against the constraint.  $\overline{P}$  $\tau_2$  $P_{\tau}$  $componet$  $T<sub>1</sub>$  $\frac{\text{comport to}}{\text{tangent to}}$ **Note**: (5) can be also written as  $t_{\rm the}$  constraint  $P_{\ddot{\theta}}\ddot{\theta} = P_{\ddot{\theta}}M^{-1}(\tau-h)$ against the component constraint  $\boldsymbol{P}_{\ddot{\theta}} = \boldsymbol{M}^{-1} \boldsymbol{P} \boldsymbol{M} = \boldsymbol{I}_n - \boldsymbol{M}^{-1} \boldsymbol{A}^\mathrm{T} \big(\boldsymbol{A} \boldsymbol{M}^{-1} \boldsymbol{A}^\mathrm{T}\big)^{-1} \boldsymbol{A} \in \mathbb{R}^{n \times n}$ rank $(\boldsymbol{P}_{\ddot{a}}) = n - k$ 

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### **Constrained Dynamics**

**Note**: For numerical simulation (forward dynamics) of the constrained robot we can use the following equations to find  $\ddot{\theta}$ .

$$
\lambda = (AM^{-1}A^{T})^{-1}(AM^{-1}(\tau - h) + \dot{A}\dot{\theta})
$$

$$
\ddot{\theta} = M^{-1}(\tau - h - A^{T}\lambda)
$$

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#### **Example**

Consider a 2R robot whose tip is constrained to move in a frictionless linear channel at  $x = 1$ . The lengths of each link are  $L_1 = L_2 = 1$ , and the point masses at the ends of each link are  $m_1 =$  $m_2 = 1$ . For simplicity, assume that  $g = 0$ . Consider the case where  $(\theta_1, \theta_2) = (-\pi/3, 2\pi/3)$  as shown, and the tip is moving with the velocity  $(\dot{x}, \dot{y}) = (0,1)$  m/s at the current configuration.

- Solve the constrained forward dynamics for  $\ddot{\boldsymbol{\theta}} = (\ddot{\theta}_1, \ddot{\theta}_2)$  and  $\lambda$ when  $\tau = (\tau_1, \tau_2)$ .
- Find the task-space constraint force  $\boldsymbol{f}_{\text{tip}} = (f_x, f_y)$ .
- Solve the constrained inverse dynamics for  $\tau$  given a  $\ddot{\theta}$  satisfying the constraint (i.e.,  $\dot{A}(\theta)\dot{\theta} + A(\theta)\ddot{\theta} = 0$ ) and  $\lambda$  satisfying a desired force  $\boldsymbol{f}_{\text{tip}} = (f_x, f_y) = (f, 0)$  against the channel.
- Find the projection  $P$ .

$$
M(\theta) = \begin{bmatrix} m_1 L_1^2 + m_2 (L_1^2 + 2L_1 L_2 \cos \theta_2 + L_2^2) & m_2 (L_1 L_2 \cos \theta_2 + L_2^2) \\ m_2 (L_1 L_2 \cos \theta_2 + L_2^2) & m_2 L_2^2 \end{bmatrix}
$$

$$
\boldsymbol{c}(\boldsymbol{\theta},\dot{\boldsymbol{\theta}})=\begin{bmatrix} -\mathfrak{m}_2 L_1 L_2 \sin \theta_2 (2\dot{\theta}_1 \dot{\theta}_2 + \dot{\theta}_2^2) \\ \mathfrak{m}_2 L_1 L_2 \dot{\theta}_1^2 \sin \theta_2 \end{bmatrix} \qquad \qquad \boldsymbol{g}(\boldsymbol{\theta})=\boldsymbol{0}
$$



 $h(\theta, \dot{\theta}) = c(\theta, \dot{\theta}) + g(\theta)$ 

There are  $n = 2$  joint coordinates and  $k = 1$  constraint.

If the tip of the robot is at  $(x, y)$ , the robot's forward kinematics can be written as

$$
\begin{bmatrix} x \ y \end{bmatrix} = \begin{bmatrix} c_1 + c_{12} \\ s_1 + s_{12} \end{bmatrix} \longrightarrow \begin{bmatrix} \dot{x} \\ \dot{y} \end{bmatrix} = \underbrace{\begin{bmatrix} -s_1 - s_{12} & -s_{12} \\ c_1 + c_{12} & c_{12} \end{bmatrix}}_{J(\theta)} \begin{bmatrix} \dot{\theta}_1 \\ \dot{\theta}_2 \end{bmatrix}
$$

$$
\longrightarrow \begin{bmatrix} \ddot{x} \\ \ddot{y} \end{bmatrix} = J(\theta)\ddot{\theta} + \underbrace{\begin{bmatrix} -\dot{\theta}_1 c_1 - (\dot{\theta}_1 + \dot{\theta}_2)c_{12} & -(\dot{\theta}_1 + \dot{\theta}_2)c_{12} \\ -\dot{\theta}_1 s_1 - (\dot{\theta}_1 + \dot{\theta}_2)s_{12} & -(\dot{\theta}_1 + \dot{\theta}_2)s_{12} \end{bmatrix}}_{j(\theta)} \begin{bmatrix} \dot{\theta}_1 \\ \dot{\theta}_2 \end{bmatrix}
$$

The constraint is  $c_1 + c_{12} = 1$ . It is holonomic and can be written as

$$
\underbrace{[-s_1 - s_{12} \ - s_{12}]}_{A(\theta)} \begin{bmatrix} \dot{\theta}_1 \\ \dot{\theta}_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}
$$

$$
\dot{A}(\theta) = \begin{bmatrix} -\dot{\theta}_1 c_1 - (\dot{\theta}_1 + \dot{\theta}_2) c_{12} \ -(\dot{\theta}_1 + \dot{\theta}_2) c_{12} \end{bmatrix}
$$

 $(\theta_1, \theta_2) = (-\pi/3, 2\pi/3)$  and  $(\dot{x}, \dot{y}) = (0, 1)$  m/s imply that  $(\dot{\theta}_1, \dot{\theta}_2) = (1, 0)$  rad/s. Thus,

 $A(\theta) = [0 - 0.866]$   $\dot{A}(\theta) = [-1 - 0.5]$ 

$$
M(\theta) = \begin{bmatrix} 2 & 0.5 \\ 0.5 & 1 \end{bmatrix}, \qquad h(\theta, \dot{\theta}) = \begin{bmatrix} 0 \\ 0.866 \end{bmatrix}
$$

#### **Constrained forward dynamics**:

$$
\lambda = (AM^{-1}A^{T})^{-1}(AM^{-1}(\tau - h) + \dot{A}\dot{\theta}) \longrightarrow \lambda = 0.289\tau_{1} - 1.155\tau_{2} - 0.167
$$
  

$$
\ddot{\theta} = M^{-1}(\tau - h - A^{T}\lambda) \longrightarrow \begin{array}{c} \ddot{\theta}_{1} = 0.5\tau_{1} + 0.289\\ \ddot{\theta}_{2} = -1.155 \end{array}
$$

**Task-space constraint forces:** 
$$
\boldsymbol{J}^{\mathrm{T}}(\boldsymbol{\theta})\boldsymbol{f}_{\mathrm{tip}} = \boldsymbol{A}^{\mathrm{T}}(\boldsymbol{\theta})\lambda \qquad \qquad \boldsymbol{J}(\boldsymbol{\theta}) = \begin{bmatrix} 0 & -0.866 \\ 1 & 0.5 \end{bmatrix}
$$
  
Since 
$$
\boldsymbol{J}(\boldsymbol{\theta})
$$
 is invertible: 
$$
\boldsymbol{f}_{\mathrm{tip}} = \boldsymbol{J}^{-\mathrm{T}}(\boldsymbol{\theta})\boldsymbol{A}^{\mathrm{T}}(\boldsymbol{\theta})\lambda \qquad \qquad \text{for all } \lambda \in \mathbb{R}^n
$$

$$
f_{\text{tip}} = \begin{bmatrix} 0.577 & -1.155 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 0 \\ -0.866 \end{bmatrix} \lambda = \begin{bmatrix} 1 \\ 0 \end{bmatrix} \lambda = \begin{bmatrix} 0.289\tau_1 - 1.155\tau_2 - 0.167 \\ 0 \end{bmatrix}
$$

This agrees with our understanding that the robot can only apply forces against the constraint in the  $f_x$ -direction.

**Note**: If  $\tau = 0$ , the task-space constraint force is  $f_{\text{tip}} = (-0.167,0)$ , meaning that the robot's tip pushes to the left on the constraint while the constraint pushes back equally to the right to enforce the constraint. In the absence of the constraint, the acceleration of the tip of the robot would have a component to the left.

#### **Constrained inverse dynamics**:

$$
\boldsymbol{\tau} = \boldsymbol{M}(\boldsymbol{\theta})\ddot{\boldsymbol{\theta}} + \boldsymbol{h}(\boldsymbol{\theta},\dot{\boldsymbol{\theta}}) + \boldsymbol{A}^{\mathrm{T}}(\boldsymbol{\theta})\lambda
$$

$$
\boldsymbol{J}^{\mathrm{T}}(\boldsymbol{\theta})\boldsymbol{f}_{\mathrm{tip}} = \boldsymbol{A}^{\mathrm{T}}(\boldsymbol{\theta})\lambda \longrightarrow \begin{bmatrix} 0 & -0.866 \\ 1 & 0.5 \end{bmatrix}^{\mathrm{T}} \begin{bmatrix} f \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ -0.866 \end{bmatrix} \lambda \longrightarrow \lambda = f
$$

$$
\ddot{A}(\theta)\dot{\theta} + A(\theta)\ddot{\theta} = \mathbf{0} \quad \longrightarrow \quad \ddot{\theta}_2 = -1.155, \ \forall \ddot{\theta}_1 \quad \longrightarrow \quad \ddot{\theta} = (\ddot{\theta}_1, -1.155)
$$

$$
\begin{array}{ll}\n\hline\n\gamma & \tau_1 = 2\ddot{\theta}_1 - 0.578 \\
\tau_2 = 0.5\ddot{\theta}_1 - 0.866f - 0.289\n\end{array}
$$

#### **Projection P:**

$$
\boldsymbol{P} = \boldsymbol{I}_n - \boldsymbol{A}^{\mathrm{T}} \big( \boldsymbol{A} \boldsymbol{M}^{-1} \boldsymbol{A}^{\mathrm{T}} \big)^{-1} \boldsymbol{A} \boldsymbol{M}^{-1} \in \mathbb{R}^{n \times n} \longrightarrow \boldsymbol{P} = \begin{bmatrix} 1 & 0 \\ 0.25 & 0 \end{bmatrix}, \qquad \boldsymbol{I}_2 - \boldsymbol{P} = \begin{bmatrix} 0 & 0 \\ -0.25 & 1 \end{bmatrix}
$$



At the current state, (i) joint torques lying in the one-dimensional subspace  $\tau_2 = 0.25\tau_1$  do not affect the constraint force, and (ii) joint torques lying in the one-dimensional subspace  $\tau_1 = 0$  do not affect the motion of the robot.

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## **Actuation and Gearing**



#### **Actuation and Gearing**

In practice, there are many types of **actuators** (e.g., electric, hydraulic, and pneumatic) and **mechanical power transformers** (e.g., gearheads). The actuators can be located at the joints themselves or remotely, with **mechanical power transmitted** by cables or timing belts.

Each combination of these has its own characteristics that can play a significant role in the "extended dynamics" mapping the actual control inputs to the motion of the robot.



• rotor attached to link  $i$  through gearhead



## **Joint and Link Flexibility**

In practice, a robot's joints and links are likely to exhibit some flexibility and vibrations.

Flexible joints and links introduce extra states to the dynamics of the robot, significantly complicating the dynamics and control.



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## **Dynamic Parameter Identification**

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#### **Dynamic Parameter Identification**

Using the dynamic equations of the manipulators for simulation and control purposes needs a good knowledge of dynamic parameters (e.g.,  $m_i.m_il_{C_x,i}$ ,  $m_il_{C_y,i}$ ,  $m_il_{C_z,i}$ ,  $\bm{I}_{b,i}$ ,  $F_{v,i}$ ,  $F_{s,i}$ ).

Different methods for identification of dynamic parameter:

- **Using CAD models** to compute the values of the inertial parameters of the various components (links, actuators, and transmissions) based on their **geometry** and **type of materials** employed (→ inaccurate due to simplification typically introduced by geometric modelling, unable to model friction parameters)
- **Dismantling components** of the manipulator and perform measurements to find the dynamic parameters ( $\rightarrow$  not easy to implement)
- **Using numerical identification techniques** which exploit the **property of linearity** of the dynamic model of open-chain manipulators ( $\rightarrow$  accurate)

$$
\boldsymbol{\tau} = \boldsymbol{M}(\boldsymbol{\theta})\ddot{\boldsymbol{\theta}} + \boldsymbol{C}(\boldsymbol{\theta},\dot{\boldsymbol{\theta}})\dot{\boldsymbol{\theta}} + \boldsymbol{g}(\boldsymbol{\theta}) + \boldsymbol{F}_{v}\dot{\boldsymbol{\theta}} + \boldsymbol{F}_{s}\operatorname{\bf sgn}(\dot{\boldsymbol{\theta}}) = \boldsymbol{Y}(\boldsymbol{\theta},\dot{\boldsymbol{\theta}},\ddot{\boldsymbol{\theta}})\boldsymbol{\pi}
$$

 $\boldsymbol{\pi} \in \mathbb{R}^p \hspace{1cm} Y \big(\boldsymbol{\theta}, \dot{\boldsymbol{\theta}}, \ddot{\boldsymbol{\theta}} \big) \in \mathbb{R}^{n \times p}$ 

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### **Dynamic Parameter Identification**

In these techniques, we impose a suitable motion trajectory, and compute the parameter vector  $\pi$  from the measurements of joint torques  $\tau$  and evaluation of the matrix Y at N time instants  $t_1, ..., t_N$  along the trajectory (typically,  $Nn \gg p$ ).

$$
\bar{\tau} = \begin{bmatrix} \tau(t_1) \\ \vdots \\ \tau(t_N) \end{bmatrix} = \begin{bmatrix} Y(t_1) \\ \vdots \\ Y(t_N) \end{bmatrix} \pi = \overline{Y}\pi \qquad \qquad \bar{\tau} \in \mathbb{R}^{Nn}
$$

$$
\bar{Y} \in \mathbb{R}^{Nn \times p}
$$

By a least-squares technique:

 $\boldsymbol{\pi} = \underbrace{(\overline{\boldsymbol{Y}}^T \overline{\boldsymbol{Y}})^{-1} \overline{\boldsymbol{Y}}^T \overline{\boldsymbol{\tau}}}$ left pseudo-inverse of  $\bar{Y}$   $\overline{Y} \in \mathbb{R}^{Nn \times p}$ (Tall Matrix)

**Remarks**:

- Assumption: Kinematic parameters in  $Y$  are known with good accuracy, e.g., after kinematic calibration.
- $\ddot{\theta}$  needs to be calculated using measurements of  $\theta$  and  $\dot{\theta}$ .
- It is possible to identify only the dynamic parameters of the manipulator that contribute to the dynamic model.
- Some parameters can be identified in linear combinations whenever they do not appear isolated in the equations.
- Trajectories should not excite any unmodelled dynamic effects such as joint elasticity or link flexibility.
- The technique can be extended to the parameter identification of an unknown payload at the end-effector.

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## **URDF**



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### **Universal Robot Description Format**

The Universal Robot Description Format (URDF) is an XML (eXtensible Markup Language) file format used by the Robot Operating System (ROS) to describe the kinematics (in defining joints), inertial properties, and link geometry of robots (in defining links) of openchain robots.

```
<joint name="joint1" type="continuous">
      <parent link="link1"/>
      <child link="link2"/>
      <origin xyz="0.5 0.3 0" rpy="0 0 0" />
      \langleaxis xyz="-0.9 0.15 0" />
</joint>
```

```
<link name="link1">
      <inertial>
            <mass value="1"/>
            <origin rpy="0.1 0 0" xyz="0 0 0"/>
            <inertia ixx="0.004" ixy="0" ixz="0"
                  iyy="0.004" iyz="0" izz="0.007"/>
      </inertial>
</link>
```


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## **URDF: Defining Joints**

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positive rotation for a revolute joint or positive translation for a prismatic joint.

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### **URDF: Defining Links**

